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## **Parallel Simulation of CO<sub>2</sub> Sequestration with Rock Deformation in Saline Aquifers**

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### **Abstract**

We developed a massively parallel reservoir simulator for modeling CO<sub>2</sub> flow and transport in saline aquifers coupled with geomechanical processes that would occur during CO<sub>2</sub> sequestration. These geomechanical processes, namely rock deformation, affect rock permeability, porosity, and bulk volume. The theories of hydrostatic and linear poroelasticity, and correlations from the literature, are used to obtain dependencies of rock permeability, porosity, and bulk volume on pore pressure and average stress. These dependencies are incorporated into the simulator mass and energy conservation equations, which determine pressure, temperature, and fluid composition. The simulator is based on the TOUGH2-MP code (Zhang et al. 2008) with the ECO2N module (Pruess, 2005), which calculates properties of H<sub>2</sub>O-NaCl-CO<sub>2</sub> mixtures. These mixtures consist of one aqueous and one CO<sub>2</sub>-rich phase, salt can precipitate and dissolve in the aqueous phase, and the mixture temperature may change. The simulator is fully implicit, three-dimensional, the grid is unstructured, and the linear equations associated with the conservation equations are solved in porous and fractured media. The simulator code is parallelized and uses MPI for processor communication, the METIS software package for domain partitioning, and the Aztec solver package for linear equation solution.

The simulator formulation, numerical implementation, and computational efficiency are verified using example problems from the literature, and options for the above dependencies are also illustrated. One example problem (Birkholzer et al., 2008) is a study of the volume influenced during and after CO<sub>2</sub> injection into a saline aquifer. Another (Rutqvist and Tsang, 2002) addresses coupled hydromechanical changes during CO<sub>2</sub> injection into an aquifer–caprock system. In this example, geomechanical processes were modeled by coupling two simulators, TOUGH2 (Pruess et al., 1999), which simulates fluid flow and heat transport, and FLAC3D (FLAC3D, 1997), which simulates rock and soil mechanics with thermomechanical and hydromechanical interactions. Finally, the last example problem (Kumar et al., 2005) is a simulation of a prototypical CO<sub>2</sub> sequestration project in a deep saline aquifer using CMG's GEM simulator (Nghiem, 2002).

### **Introduction**

Geological sequestration of CO<sub>2</sub> in deep saline aquifers is a primary option for reducing anthropogenic CO<sub>2</sub> emissions into the atmosphere. Deep saline aquifers are widely distributed, contain high salinity water that is unfit for human consumption, and can accommodate large volumes of CO<sub>2</sub>. CO<sub>2</sub> is injected into these aquifers as a supercritical fluid with a liquid-type density and a gas-type viscosity. The critical point of CO<sub>2</sub>, 31.1 °C and 7.4 MPa, corresponds to an aquifer depth of about 800 m. Sequestration is achieved by trapping supercritical CO<sub>2</sub> in the aquifer pore spaces (either as a separate phase trapped beneath impermeable rock or through capillary forces where CO<sub>2</sub> is an immobile phase), dissolution of CO<sub>2</sub> in the saline aqueous phase (which is dependent on pressure, temperature, and salinity), and reaction of CO<sub>2</sub> with minerals present in the rock. Reactions with minerals require a much longer time scale than the other sequestration mechanisms and are not considered in this paper.

Numerical simulation of CO<sub>2</sub> sequestration is an active research area. Two simulators that have been used extensively for CO<sub>2</sub> sequestration modeling are GEM<sup>TM</sup> (Nghiem et al., 2001) and the TOUGH2 family of codes (Pruess et al. 1999; Pruess, 2005; Zhang et al. 2007). These simulators model flow in porous media with convection and dispersion, and equilibrium between phases and components. Geomechanical effects are also important to consider in CO<sub>2</sub> sequestration simulation because injection results in pressure increases and changes in reservoir stresses and strains that effect rock transport properties and could cause rock to fracture, allowing CO<sub>2</sub> to leak into the surroundings. Nghiem et al. (2004), Settari and

Mourits (1998), and others have included geomechanical effects in those flow simulations by coupling a porous media flow simulator to a geomechanical one. In this coupling, the porous media and geomechanical models run concurrently and periodically exchange information common to both, such as porosity and volume, in order to calculate solutions that are consistent with one another.

We take a different and simpler approach to including geomechanical effects in porous media flow simulations. Terzaghi, (1936) first introduced the concept of effective stress, the difference between average stress and pore pressure, during his studies of the mechanics of saturated soils. This concept was further refined by Biot (1941) and others. Theories of poroelasticity (Geertsma, 1957; Carrol and Katsube, 1983; Zimmerman 1991) have related rock properties such as porosity to effective stress, and experimental studies (e.g., Nur and Byerlee, 1971) have supported these relations. The dependence of permeability on porosity has had numerous investigators (Bear, 1972) and an early example is the Carman-Kozeny hydraulic radius model. In addition, Gobran et al. (1987) concluded that permeability is dependent on the difference between confining pressure and pore pressure (effective stress) but not on their actual values. We incorporate geomechanical effects in the mass and energy balances of a conventional reservoir simulator by adding effective stress dependence of porosity and permeability, and related properties. These dependencies are obtained from theories of poroelasticity and empirical correlations from the literature. We also make the simplifying assumption of a time-invariant stress field.

## TOUGH2 Simulators

Our simulator is a modification of TOUGH2-MP (Zhang et al. 2008), a massively parallel version of TOUGH2 (Pruess et al. 1999). TOUGH2 is a numerical simulator of multi-component, multiphase fluid and heat flow in porous and fractured media. TOUGH2 was designed primarily for applications in geothermal reservoir engineering, nuclear waste disposal, and environmental assessment and remediation. In the TOUGH2 formulation, fluid advection is described with a multiphase extension of Darcy's law and there is diffusive mass transport in all phases. Heat flow occurs by conduction and convection, and includes sensible as well as latent heat effects. Phases are in local equilibrium. TOUGH2 solves mass and energy balances over the simulation domain using the integral finite difference method (Narasimhan and Witherspoon, 1976) on an unstructured grid. The integral form of these balances is

$$\frac{d}{dt} \int M^k dV = \int \bar{F}^k \cdot \hat{n} d\Gamma + \int q^k dV \quad (1)$$

where, for component k,  $M^k$  is mass in V,  $q^k$  is source or sink,  $\bar{F}^k$  is flux through  $\Gamma$ , the boundary of V, and  $\hat{n}$  is the outward unit normal vector to  $\Gamma$ . Mass accumulation is a sum over phases

$$M^k = \phi \sum_j S_j \rho_j X_j^k \quad (2)$$

where  $\phi$  is porosity,  $S$  is phase saturation,  $\rho$  is mass density, and  $X$  is mass fraction of component k. Energy accumulation,  $M^{N+1}$ , is

$$M^{N+1} = (1 - \phi) C_r \rho_r T + \phi \sum_j S_j \rho_j u_j \quad (3)$$

where  $\rho_r$  is rock density,  $C_r$  is rock specific heat,  $T$  is temperature, and  $u$  is phase specific internal energy. The integral finite difference method replaces volume integrals with volume averages,

$$\int M^k dV = \bar{M}^k V \quad (4)$$

and surface integrals with surface averages

$$\int \bar{F}^k \cdot \hat{n} d\Gamma = \sum_m A_m F_m^k \quad (5)$$

Mass fluxes are summed over phases and have advective and diffusive portions. The time derivative in Equation 1 is replaced by a standard first order finite difference approximation, the fluxes are fully implicit, and the resulting set of nonlinear algebraic equations shown below are solved using the Newton-Raphson method

$$R^{n+1} = M^{k,n+1} - M^{k,n} - \frac{\Delta t}{V} \left\{ \sum_m A_m F_m^{k,n+1} + V q^{k,n+1} \right\} = 0 \quad (6)$$

where n is time level.

TOUGH2 consists of functional units, such as a grid generator and a physical property module, with flexible and transparent interfaces. The physical property module is ECO2N (Pruess, 2005; Pruess and Spycher, 2007). ECO2N was designed for CO<sub>2</sub> sequestration in saline aquifers. It includes a description of the relevant properties of H<sub>2</sub>O–NaCl–CO<sub>2</sub> mixtures that is highly accurate for the temperature, pressure, and salinity conditions of interest (between 10 and 110 °C, pressure less than 600 bar, and salinity up to full halite saturation). An aqueous and a CO<sub>2</sub>-rich phase may be present, and salt may be present in the aqueous phase or as a solid precipitate. ECO2N can model super- as well as sub-critical conditions, but does not make the distinction between liquid and gaseous CO<sub>2</sub>.

The highlights of TOUGH2-MP (Zhang et al. 2008), the massively parallel version of TOUGH2, are domain partitioning, and parallel assembly and solution of the Jacobian matrix. Domains are partitioned using the METIS package with three partitioning algorithm options, K-Way, VK-Way, and Recursive. Each processor computes Jacobian matrix elements for its own grid blocks. Exchange of information between processors allows calculation of Jacobian matrix elements associated with inter-block connections across domain partition boundaries. The Jacobian matrix is solved in parallel using an iterative linear solver from the Aztec package. Different solver options, such as conjugate gradient and generalized minimum residual, are available.

### Rock Deformation Model

Our rock deformation model is based on the concept of effective stress. Effective stress was initially defined as the difference between average stress and pore pressure by Terzhagi (1936) and was generalized by Biot and Willis (1957) as

$$\sigma' = \sigma_m - \alpha P \quad (7)$$

where  $\alpha$  is the Biot or effective stress coefficient. We approximate average stress as the overburden stress

$$\sigma_m = P_{atm} + \int_0^z \left( (1 - \phi)\rho_r + \phi \sum_p S_p \rho_p \right) g dz \quad (8)$$

or we input the spatial average stress distribution. Permeability and porosity are both dependent on effective stress

$$k = k(\sigma') \quad (9)$$

$$\phi = \phi(\sigma') \quad (10)$$

Since bulk volume is related to porosity, we also allow bulk volume to depend on effective stress and pore pressure

$$V_b = V_b(\sigma', P) \quad (11)$$

In addition, permeability and porosity are used to scale capillary pressure according to the relation by Leverett (1941)

$$P_c = P_{c0} \frac{\sqrt{(k/\phi)_0}}{\sqrt{(k/\phi)}} \quad (12)$$

where subscript 0 refers to reference conditions.

### Property Correlations

A theory of hydrostatic poroelasticity (Zimmerman et al. 1986) has been proposed that accounts for the coupling of rock deformation with fluid flow inside the porous rock. Porous rock has a bulk and a pore volume, and those volumes are acted on by pore pressure and average stress. Four compressibilities are written in terms of those quantities, for example

$$C_{bc} = \frac{-1}{V_b} \left( \frac{\partial V_b}{\partial \sigma_m} \right)_p \quad (13)$$

where subscript b refers to bulk volume. Relationships between these compressibilities are derived for an idealized porous medium and from that, dependence of porosity on effective stress

$$d\phi = -[C_{bc}(1 - \phi) - C_r]d\sigma' \quad (14)$$

where  $C_r$  is rock grain compressibility, an expression for the Biot coefficient

$$\alpha = 1 - \frac{C_r}{C_{bc}} \quad (15)$$

and dependence of bulk volume on pore pressure and effective stress

$$dV_b = -V_b C_{bc} d\sigma' + C_r dP \quad (16)$$

Rutqvist et al. (2002) presented the following function for porosity, obtained from laboratory experiments on sedimentary rock by Davies and Davies (1999)

$$\phi = \phi_r + (\phi_0 - \phi_r)e^{-a\sigma'} \quad (17)$$

where  $\phi_0$  is zero effective stress porosity,  $\phi_r$  is high effective stress porosity, and the exponent  $a$  is a parameter. They also presented an associated function for permeability in terms of porosity

$$k = k_0 e^{c\left(\frac{\phi}{\phi_0} - 1\right)} \quad (18)$$

where  $k_0$  is zero stress permeability and the exponent  $c$  is a parameter. For fractured media, they defined an aperture width  $b_k$  for direction  $k$  as

$$b_k = b_{0,k} + \Delta b_k (e^{-d\sigma'} - e^{-d\sigma'_0}), k = x, y, z \quad (19)$$

where subscript 0 refers to initial conditions,  $\Delta b_k$  is the aperture change, and the exponent  $d$  is a parameter. Porosity is correlated to changes in  $b_k$  as

$$\phi = \phi_0 \frac{b_1 + b_2 + b_3}{b_{1,0} + b_{2,0} + b_{3,0}} \quad (20)$$

and direction  $k$  permeability is correlated to fracture aperture of other directions  $l$  and  $m$  as

$$k_k = k_{k,0} \frac{b_l^3 + b_m^3}{b_{l,0}^3 + b_{m,0}^3} \quad (21)$$

McKee et al. (1988) derived a relationship between porosity and effective stress from hydrostatic poroelasticity theory by assuming incompressible rock grains

$$\phi = \phi_0 \frac{e^{-c_p(\sigma' - \sigma'_0)}}{1 - \phi_0(1 - e^{-c_p(\sigma' - \sigma'_0)})} \quad (22)$$

where  $c_p$  is average pore compressibility. A relationship between permeability and effective stress was obtained from the Carman-Kozeny equation

$$k \propto \frac{\phi^3}{(1 - \phi)^2} \quad (23)$$

and the above relationship for porosity. These relationships fit laboratory and field data for granite, sandstone, clay, and coal.

Ostensen (1986) studied the relationship between effective stress and permeability for tight gas sands and approximated permeability as

$$k^n = D \ln \frac{\sigma'^*}{\sigma'} \quad (24)$$

where  $n$  is 0.5,  $D$  is a parameter, and  $\sigma'^*$  is effective stress for zero permeability, obtained by extrapolating measured square root permeability versus effective stress on a semi-log plot.

Verma and Pruess (1988) presented a power law expression relating permeability to porosity

$$\frac{k - k_c}{k_0 - k_c} = \left( \frac{\phi - \phi_c}{\phi_0 - \phi_c} \right)^n \quad (25)$$

where  $k_c$  and  $\phi_c$  are asymptotic values of permeability and porosity, respectively, and exponent  $n$  is a parameter.

The porosity correlations described in this section are summarized in Table 1 and the permeability correlations in Table 2.

**Table 1. Porosity correlations.**

Option	Source	Equation
1	(Zimmerman, 1986) poroelasticity	14, 16*
2	Rutqvist et al. (2002), sedimentary rock	17
3	Rutqvist et al. (2002), fractures	20
4	McKee (1988)	22

\* Equation for bulk volume change

**Table 2. Permeability correlations.**

Option	Source	Equation
1	Rutqvist et al. (2002), sedimentary rock	18
2	Rutqvist et al. (2002), fractures	21
3	Carman-Kozeny	23
4	Ostensen (1986)	24
5	Verma and Pruess (1988)	25

## Example Simulations and Discussion

We describe simulations of CO<sub>2</sub> injection into saline aquifers with geomechanical effects. In our first set of simulations, we illustrate some of the capabilities of our simulator and how rock deformation affects results. In our second set, we match some results from a coupled multiphase flow-rock deformation simulation. In our third set, we refine the grid of a published simulation to illustrate the capabilities of the parallel code to run large problems.

Birkholzer et al. (2008) studied the volume influenced during and after CO<sub>2</sub> injection into a saline aquifer. CO<sub>2</sub> injection into a saline aquifer causes pressure perturbations and brine migration that can extend beyond the CO<sub>2</sub> plume itself and can potentially interact with shallow groundwater resources nearby. They represented the saline aquifer system as a two-dimensional radially symmetric volume that consists of alternating aquifer and aquitard layers. The bottom layer is an aquifer which is bounded underneath by impermeable rock and above by an aquitard. Above the aquitard is another aquifer, and so on up to the surface. Each aquifer is 60 m thick, each aquitard is 100 m thick, and there are seven aquitards and eight aquifers. The aquifer radius, 200 km, is large enough to minimize boundary effects. Fluid can escape through the radial boundary, which is maintained at hydrostatic pressure. CO<sub>2</sub> is injected into the bottom aquifer at 1.52 million tonnes per year for 30 years, followed by a 70-year post injection period. Temperature varies linearly from 15 °C at the top to 38.6 °C at the bottom. Salinity for the top 540 m is zero, and below that increases linearly to 0.144 NaCl mass fraction. All aquifers have the same properties, as well as all aquitards. Both are slightly compressible, and additional details of their properties are given in the reference.

We reran their base case, which has an aquifer permeability of 10<sup>-13</sup> m<sup>2</sup>, an aquitard permeability of 10<sup>-18</sup> m<sup>2</sup>, and a pore compressibility of 4.5 × 10<sup>-10</sup> Pa<sup>-1</sup>, on a 200×74 grid. We found agreement with their published results. We then ran this case with our effective stress-dependent permeability and porosity options and used Equation 8 for the average stress. Our first case was Porosity Option 2 from Table 1 and constant permeability. The zero-stress porosity in Equation 17 is five percent greater than the initial (0.20 for the aquifer and 0.05 for the aquitard), the exponential parameter is 5×10<sup>-8</sup> Pa<sup>-1</sup>, and the high-stress porosity is calculated from the initial and zero-stress values. Figure 1 shows the percent increase of porosity after 30 years of injection. The porosity increase lies mainly in the bottom aquifer region, from 1120-1180 m, and the aquitard above that, from 1020-1120 m. Our second case was Porosity Option 4 from Table 1 and constant permeability. The average pore compressibility in Equation 22 is equal to the base case pore compressibility (4.5×10<sup>-10</sup> Pa<sup>-1</sup> for aquifer, 9.0×10<sup>-10</sup> Pa<sup>-1</sup> for aquitard). Figure 2 shows the percent increase of porosity for this case. This result is very similar to the base case increase, which is omitted for brevity. In this case as well as the base case, porous media are treated as slightly compressible, and the porosity increase was relatively small. The first case porosity was from a fit to laboratory data on sandstone compression, which is a complex phenomenon that involves rearrangement, as well as compression, of individual rock grains. In this case, the porosity increase was relatively large.

We ran three additional cases with Porosity Option 2 from Table 1 and Permeability Options 1, 3, and 5 from Table 2. For Permeability Option 1, the exponent *c* was 22.2 from Rutqvist et al. (2002). Permeability Option 3 requires no parameters and for Permeability Option 5, the exponent *n* was 1.4, *k<sub>v</sub>/k<sub>o</sub>* was 0.45, and  $\frac{\sigma_v}{\sigma_o}$  was 0.9 (from Verma and Pruess, 1988). Figures 3-5 show the percent permeability increase after 30 years of CO<sub>2</sub> injection for the respective permeability options. Figure 3 shows the most sensitivity to increasing porosity, Figure 5 shows an intermediate amount, and Figure 4 shows the least. One effect of permeability increasing with porosity is decreasing pressure buildup in the vicinity of the injector. Figures 6 and 7 show pressure buildup at 30 years injection for the base case (no permeability increase) and the Permeability Option 1 case. Rock fracturing during CO<sub>2</sub> sequestration is undesirable since fractures could provide an avenue

of escape for CO<sub>2</sub> trapped under caprock. The lower pressure buildup predicted from including these geomechanical effects would allow for a higher injection rate than otherwise.

Rutqvist and Tsang (2002) simulated CO<sub>2</sub> injection into a hypothetical aquifer-caprock system covered by semi-permeable shale. They coupled two computer codes, TOUGH2 for multiphase flow and heat transport, and FLAC3D (FLAC3D, 1997) for rock deformation, to study the hydraulic, mechanical, and hydromechanical changes during injection including the spread of the CO<sub>2</sub> plume, effective stress and permeability changes, and ground surface uplift. The two codes were coupled through correlating porosity as a function of effective stress and permeability as a function of porosity, Porosity Option 2 and Permeability Option 2. FLAC3D calculates stress tensor components in the simulation volume and effective stress is calculated using the mean of the normal stress components.

The aquifer is 200 m thick and is bounded above by 100 m thick caprock. Above the caprock is a homogeneous formation that extends to the surface and below the aquifer is also caprock. The aquifer properties are that of sandstone and the caprock's are that of shale. The system is two-dimensional and effectively infinite in lateral extent. We ran their homogeneous caprock case using Porosity Option 1 and Permeability Option 1 on a 201x100 grid. The injector was located at the aquifer bottom and at the lateral midpoint, and CO<sub>2</sub> was injected at 0.05 kg/sec for 30 years. Bulk volume compressibility used in Equation 14 was  $5.5 \times 10^{-10} \text{ Pa}^{-1}$  for the aquifer and  $5.0 \times 10^{-11} \text{ Pa}^{-1}$  for the caprock, rock grain compressibility was zero, and other input properties can be found in the reference. Figures 8-10 show the CO<sub>2</sub> plume at 1, 3, and 10 years, respectively. These agree well with the reference, shown in Figure 11. Porosity Option 1 includes bulk volume change. This was used to calculate ground surface uplift by assuming uniform volume change in all directions. Figure 12 shows this uplift at 1, 3, and 10 years and Figure 13 shows the reference results. Both are very similar. Figure 14 shows the permeability changes at 10 years. Most of the permeability changes are in the vicinity of the injector. In the reference, permeability changes are there and along the upper and lower aquifer-caprock interfaces, shown in Figure 15. We were not able to match permeability change there since our calculations assume constant stress.

Kumar et al. (2005) simulated a hypothetical CO<sub>2</sub> injection project into a deep saline aquifer to better understand and quantify CO<sub>2</sub> storage mechanisms. They studied the impact of parameters such as permeability, residual gas saturation, salinity, and temperature on CO<sub>2</sub> storage. Their base case was an aquifer 304.8 m thick and 16,154 m in length and width, with a one degree dip. Porosity was 0.25, temperature was 60 °C, and there were ten horizontal strata with varying permeability with the lower half being greater than the upper. 27.6 kg/sec CO<sub>2</sub> was injected for fifty years in a well located at the areal center and perforated along the lower half of the reservoir, followed by thousands of years of equilibration. Constant pressure wells were situated along the boundaries to model an open aquifer. The reference contains additional details.

We ran their base case with a finer grid to demonstrate the parallel code's ability to run larger simulations. We used a Dell PC with eight Intel® Xeon® E5405 2.0 GHz processors with total memory of 15.7 GB, and a Linux operating system. Our grid was 80x80x80, with 512,000 active grid blocks. We ran 50 years of CO<sub>2</sub> injection followed by 1,000 years of equilibration; the simulation took about 18 hours. Figure 16 shows CO<sub>2</sub> saturation at 50 years for an xz-direction cross section containing the injector. The CO<sub>2</sub> plume is fairly symmetric except for the higher permeability layers where it already is moving up dip (towards smaller x-values). Figure 17 shows CO<sub>2</sub> saturation at 1,000 years for the same cross section. The up dip CO<sub>2</sub> migration is more pronounced, the CO<sub>2</sub> saturation profile is more diffuse, and there is CO<sub>2</sub> accumulation in the lower permeability zone above the bottom five perforated ones.

## Summary and Conclusions

We developed a massively parallel reservoir simulator based on the TOUGH2-MP code with the ECO2N module for modeling CO<sub>2</sub> flow and transport in saline aquifers coupled with geomechanics. We incorporated into the simulator mass and energy conservation equations dependencies of rock permeability, porosity, and bulk volume on pore pressure and average stress, obtained from the theories of hydrostatic and linear poroelasticity and correlations from the literature.

We verified the simulator formulation, numerical implementation, and computational efficiency using example problems from the literature. We used a study of CO<sub>2</sub> injection into a saline aquifer to compare results from various porosity and permeability dependencies on effective stress, and found that they differ based on the physical assumptions behind the porosity and permeability dependencies. We compared our results to those from two coupled computer codes, one that simulates fluid flow and heat transport, and another that simulates rock deformation. We obtained a good match of the CO<sub>2</sub> plume and surface uplift at various times, indicating that our formulation is able to capture effects modeled by the more rigorous coupled simulation, but noted limitations on the permeability match. We reran a simulation on a finer grid, illustrating the parallel code's ability to run larger problems.

## Nomenclature

A = area, m<sup>2</sup>

$b_i$  = i-direction fracture aperture, m

C = compressibility, Pa<sup>-1</sup>

g = gravitational acceleration, m/sec<sup>2</sup>

$k$  = permeability,  $m^2$   
 $F$  = component mass flux, kg/sec  
 $M$  = component mass, kg  
 $P$  = pore pressure, Pa  
 $P_{atm}$  = atmospheric pressure, Pa  
 $P_c$  = capillary pressure, Pa  
 $q$  = component generation, kg/sec  
 $S$  = phase saturation  
 $T$  = temperature, °K  
 $u$  = phase specific internal energy, J/kg  
 $V$  = volume,  $m^3$   
 $X$  = phase mass fraction

$\alpha$  =biot coefficient  
 $\Gamma$  = surface area,  $m^2$   
 $\rho$  = density,  $kg/m^3$   
 $\sigma_m$  = mean stress, Pa  
 $\sigma'$  = effective, stress, Pa  
 $\phi$  = porosity

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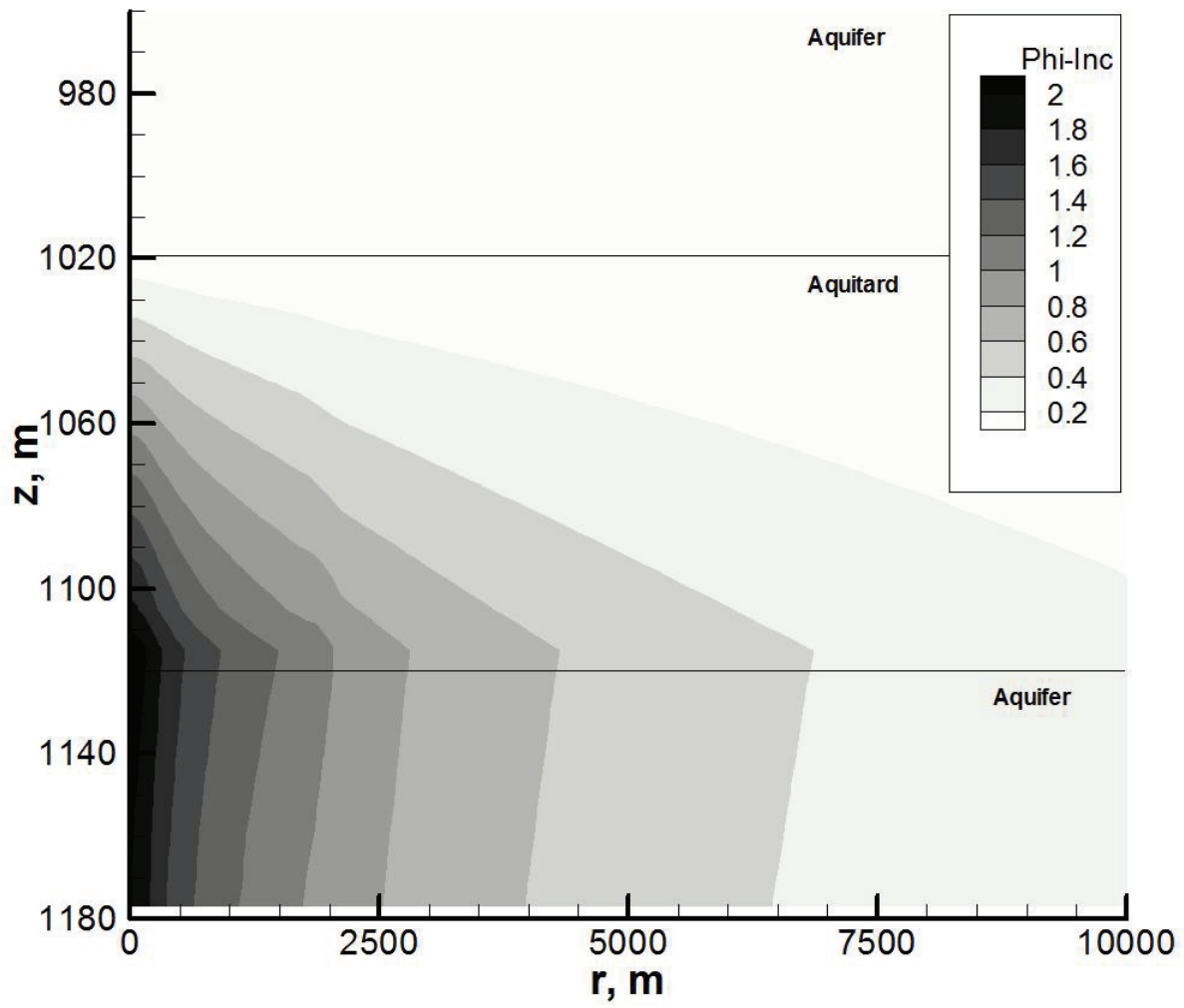


Figure 1: Percent increase of porosity after 30 years of injection; modified Birkholzer et al. (2008) simulation using Porosity Option 2 from Table 1 and constant permeability.

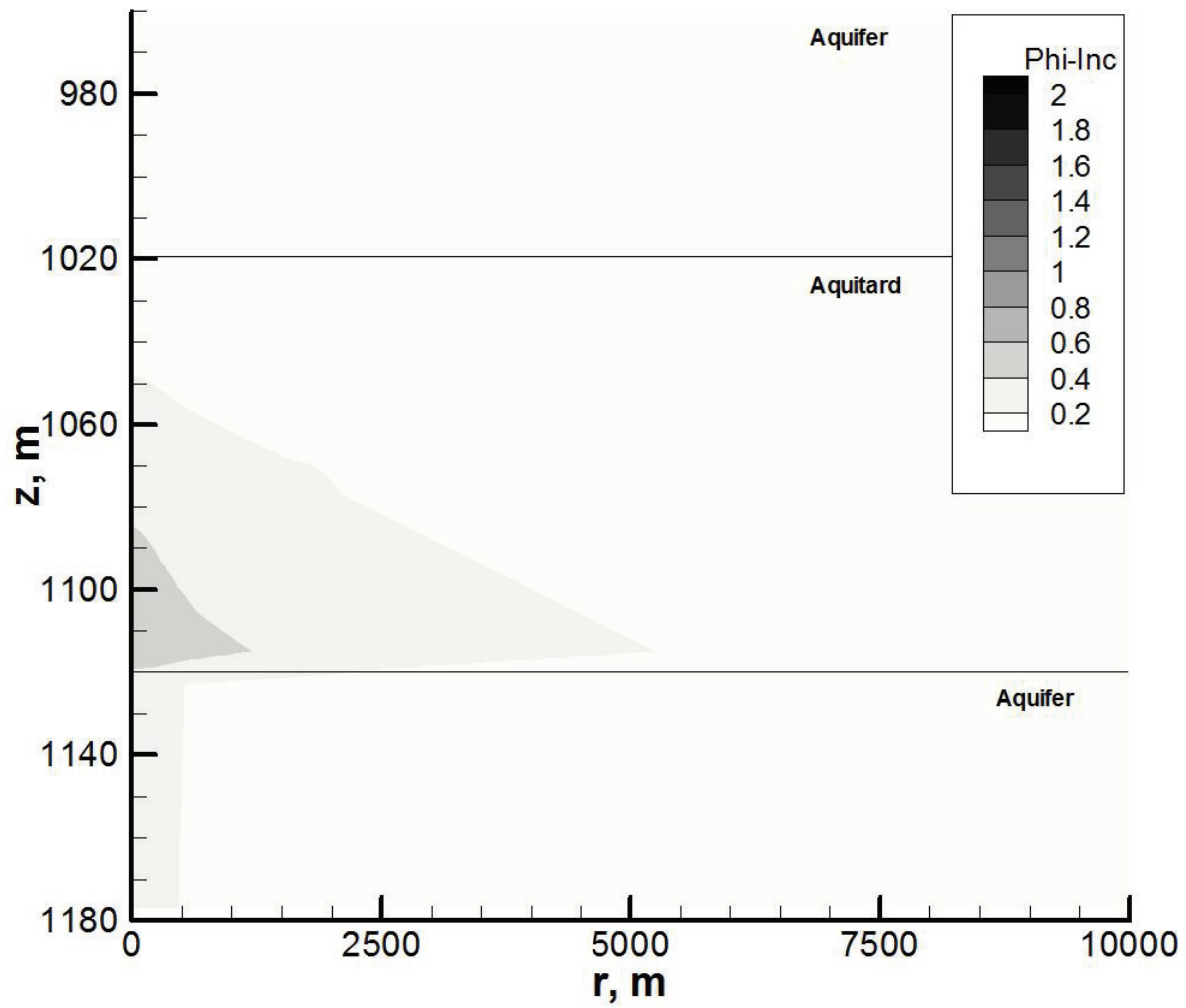


Figure 2: Percent increase of porosity after 30 years of injection; modified Birkholzer et al. (2008) simulation using Porosity Option 4 from Table 1 and constant permeability.

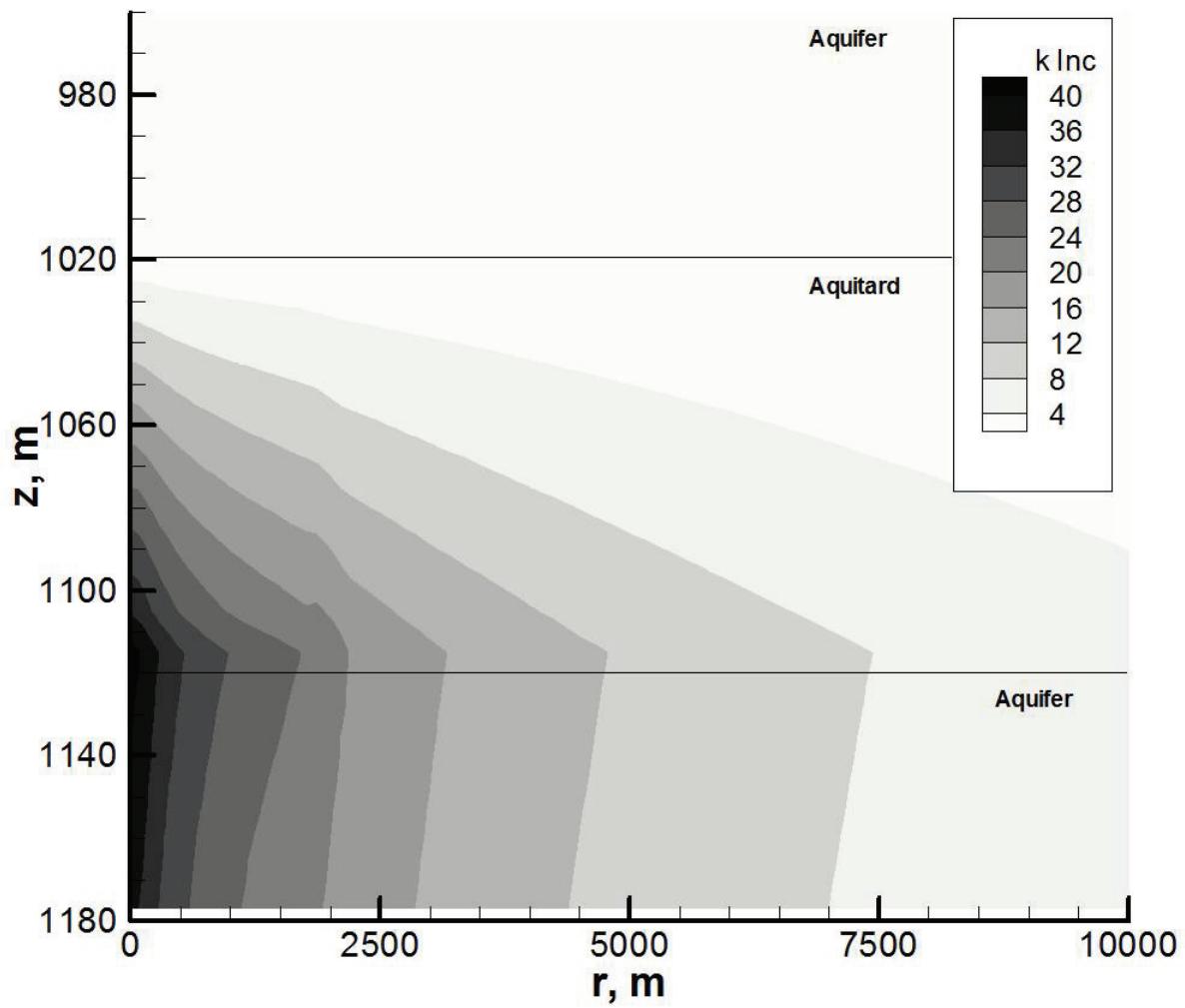


Figure 3: Percent increase of permeability after 30 years of injection; modified Birkholzer et al. (2008) simulation using Porosity Option 4 from Table 1 and Permeability Option 1 from Table 2.

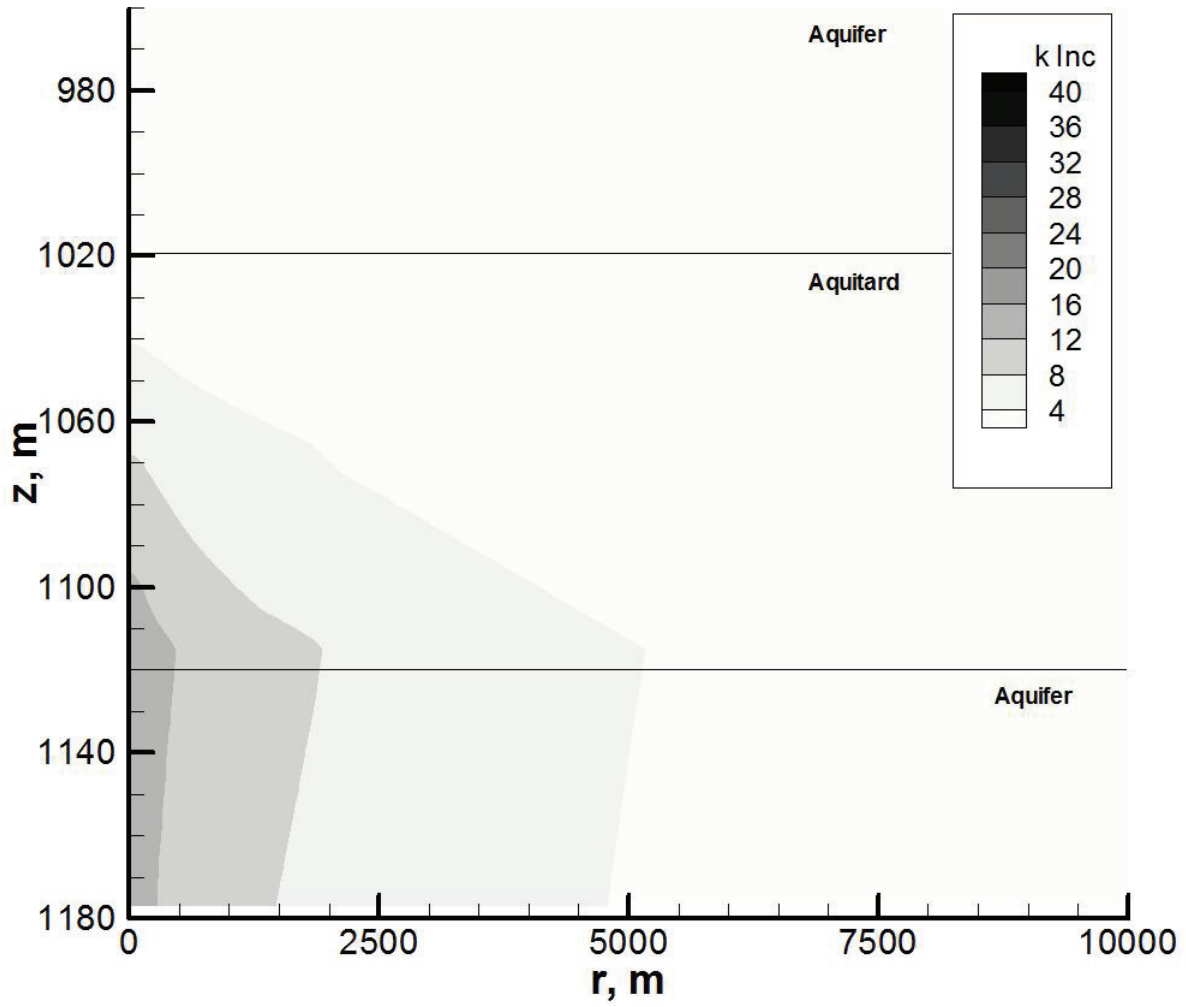


Figure 4: Percent increase of permeability after 30 years of injection; modified Birkholzer et al. (2008) simulation using Porosity Option 4 from Table 1 and Permeability Option 3 from Table 2.

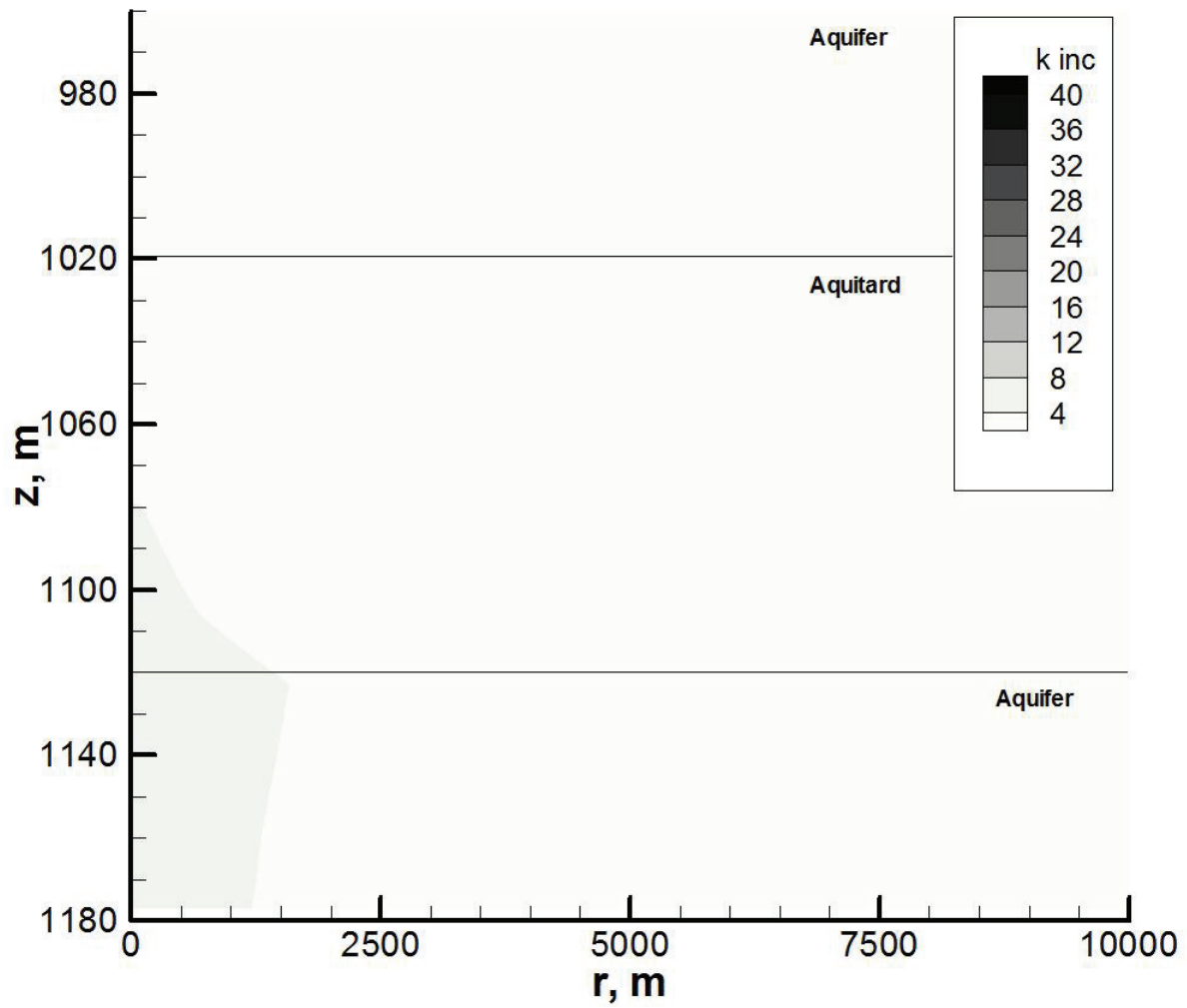


Figure 5: Percent increase of permeability after 30 years of injection; modified Birkholzer et al. (2008) simulation using Porosity Option 4 from Table 1 and Permeability Option 5 from Table 2.

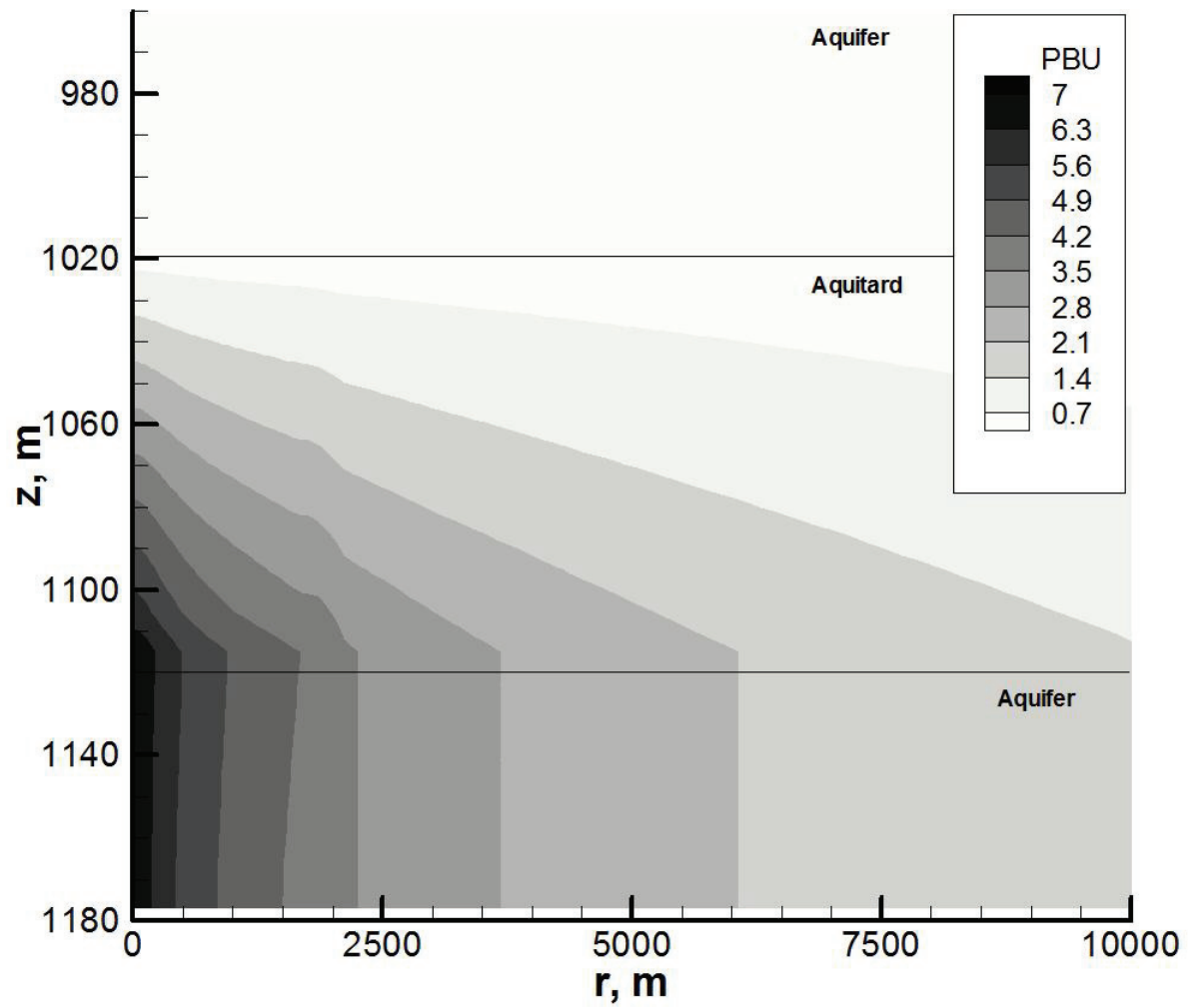


Figure 6: Pressure buildup, MPa, at 30 years injection; Birkholzer et al. (2008) simulation base case with constant permeability and porosity.

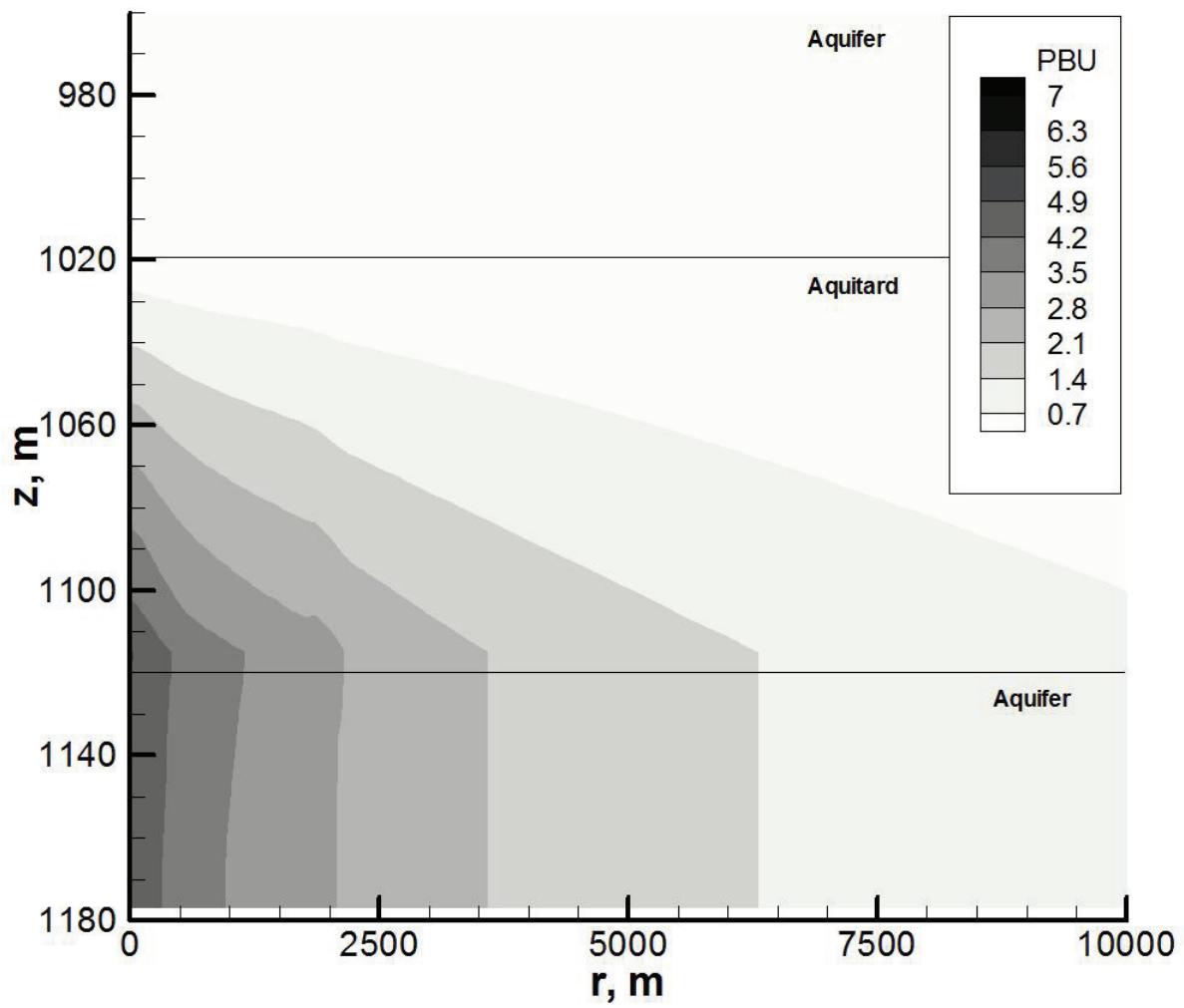


Figure 7: Pressure buildup, MPa, at 30 years injection; modified Birkholzer et al. (2008) simulation using Porosity Option 2 from Table 1 and Permeability Option 1 from Table 2.

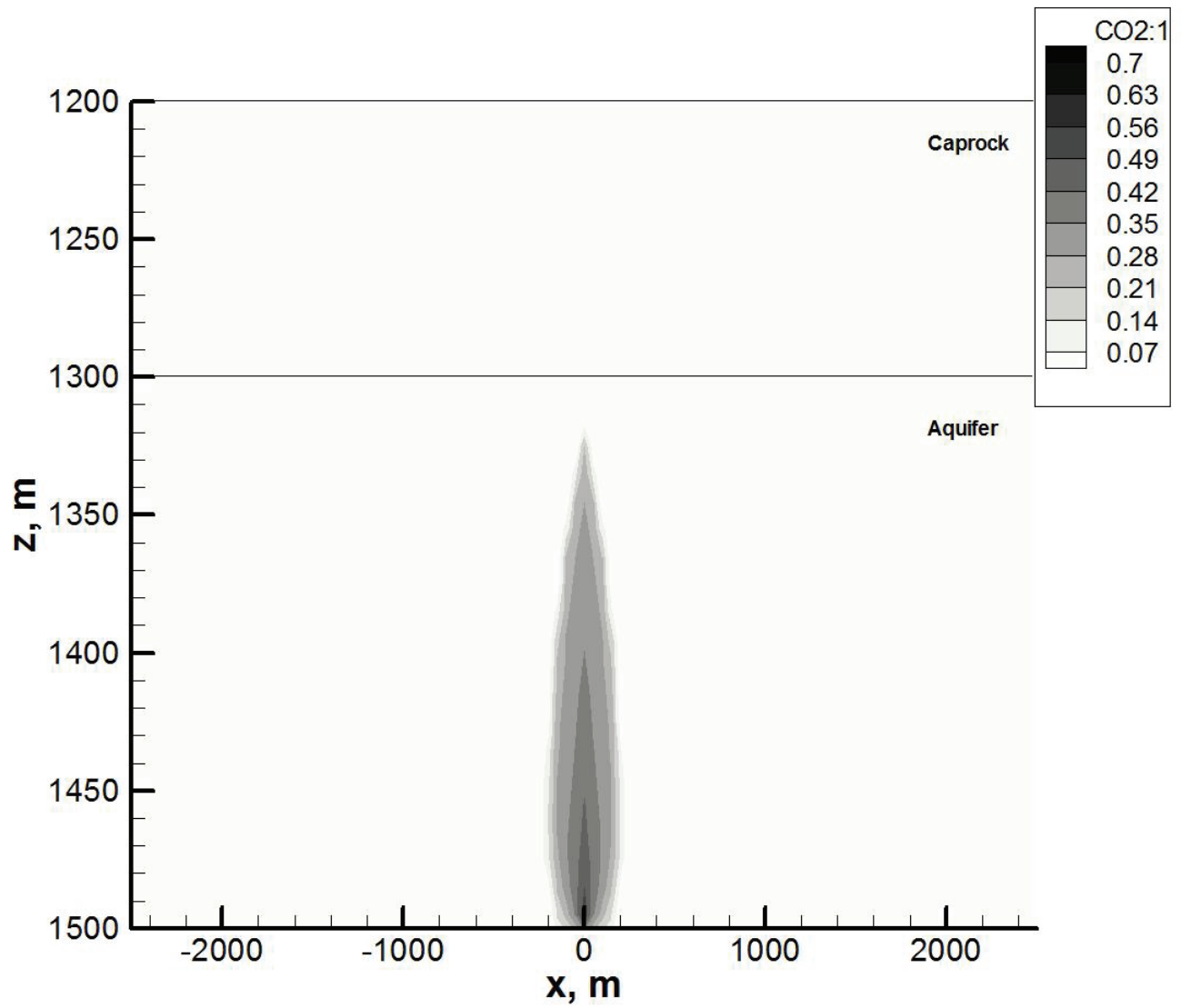


Figure 8: CO<sub>2</sub> saturation profile at 1 year; modified Rutqvist and Tsang (2002) simulation using Porosity Option 1 from Table 1 and Permeability Option 1 from Table 2.



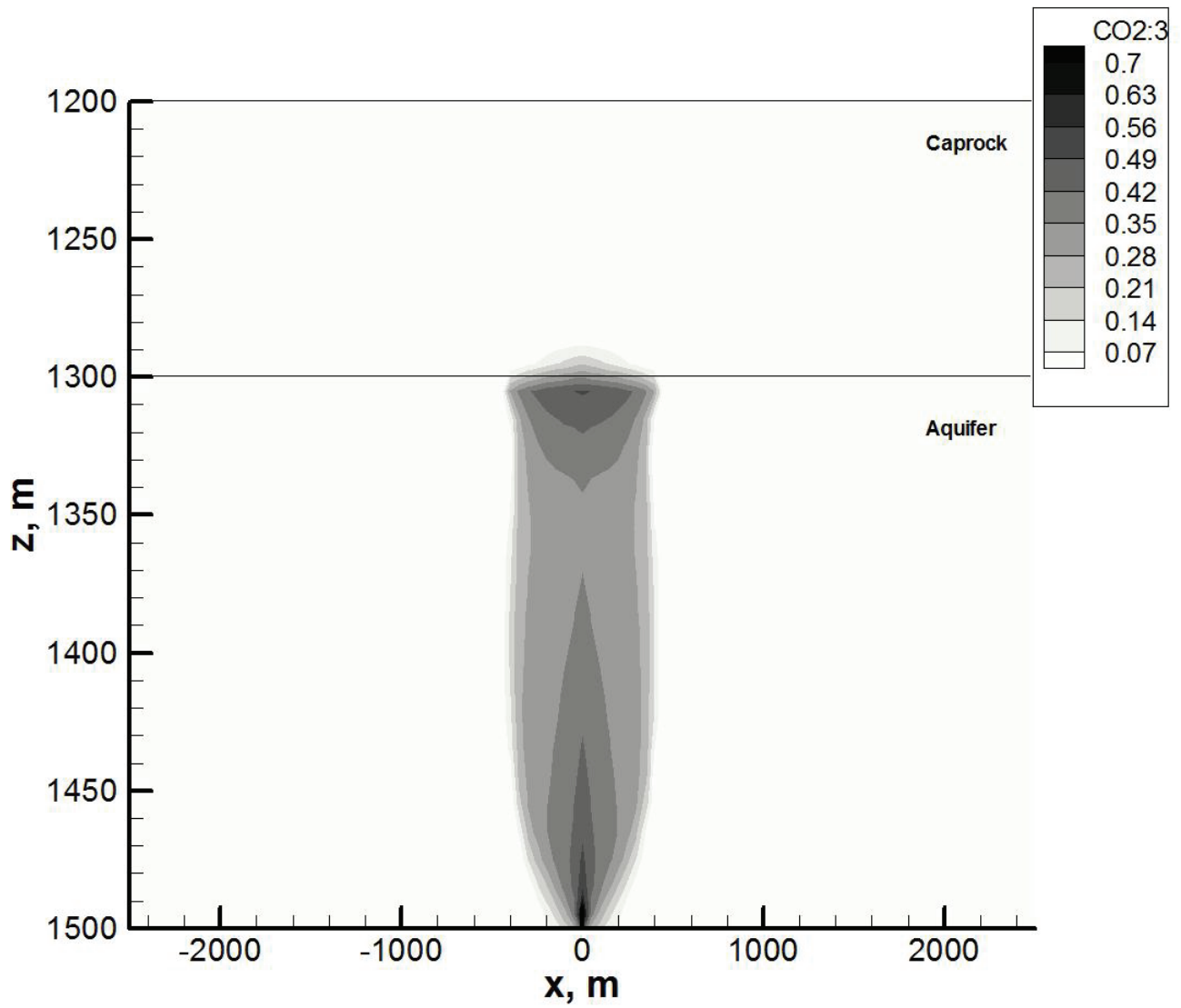


Figure 9: CO<sub>2</sub> saturation profile at 3 years; modified Rutqvist and Tsang (2002) simulation using Porosity Option 1 from Table 1 and Permeability Option 1 from Table 2.

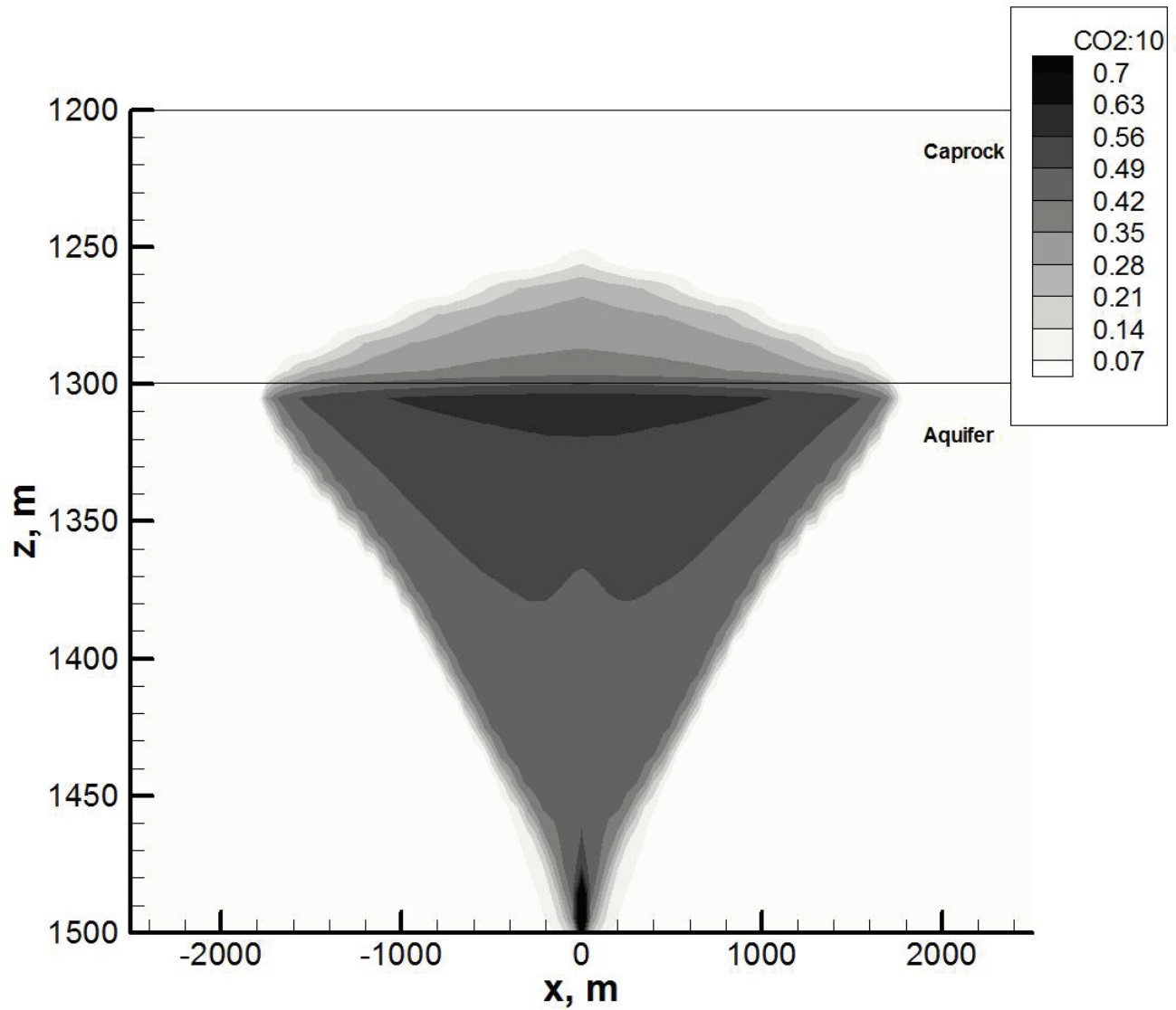


Figure 10: CO<sub>2</sub> saturation profile at 10 years; modified Rutqvist and Tsang (2002) simulation using Porosity Option 1 from Table 1 and Permeability Option 1 from Table 2.

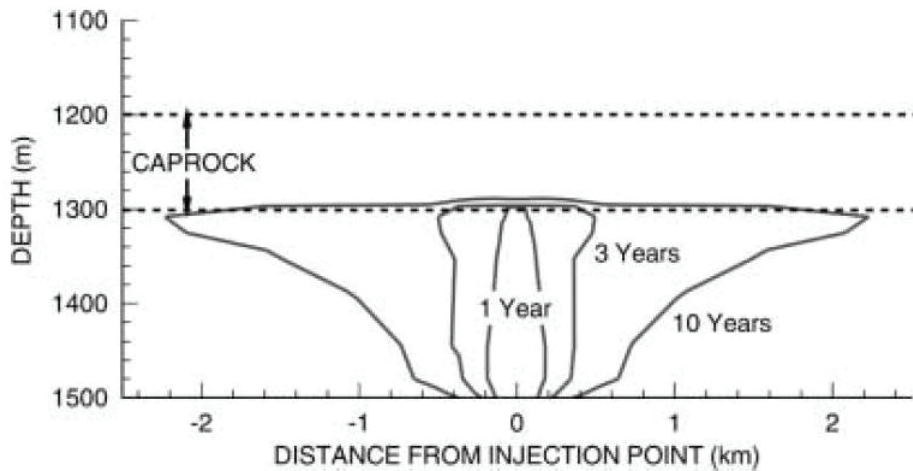


Figure 11: Rutqvist and Tsang (2002) CO<sub>2</sub> saturation profile at 1, 3, and 10 years.

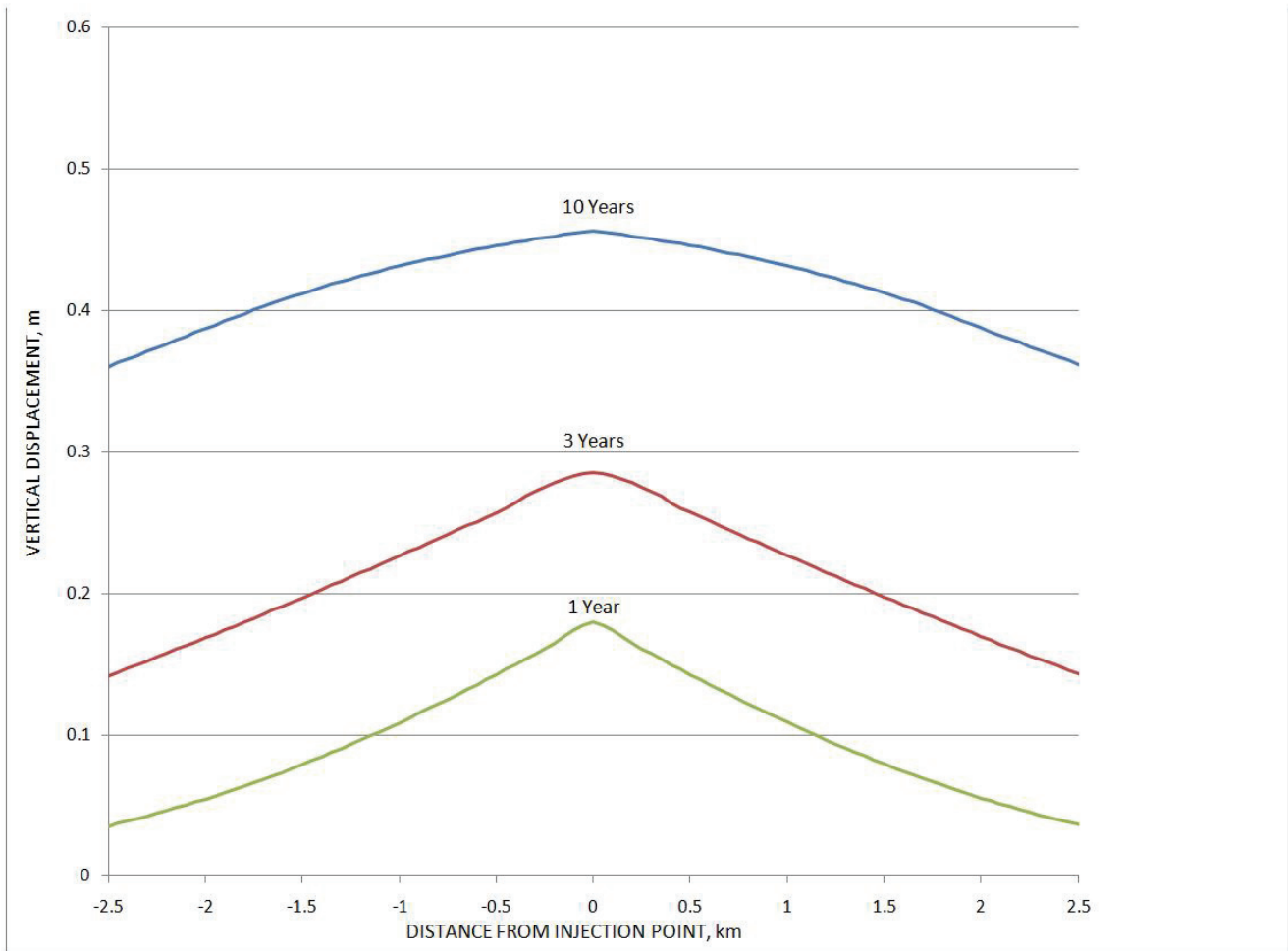


Figure 12: Surface uplift at 1, 3, and 10 years; modified Rutqvist and Tsang (2002) simulation using Porosity Option 1 from Table 1 and Permeability Option 1 from Table 2.

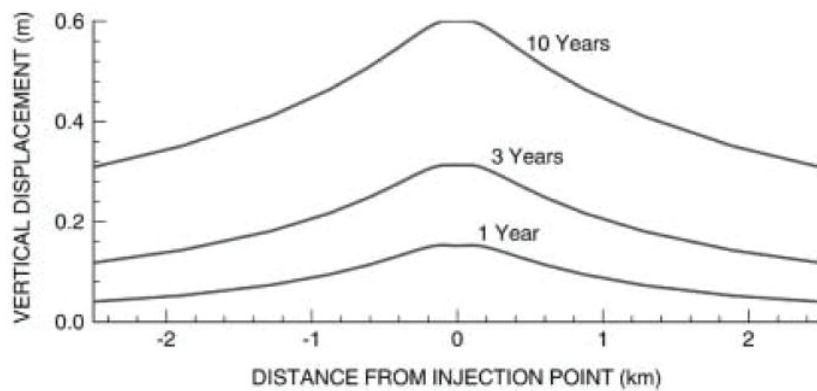


Figure 13: Rutqvist and Tsang (2002) surface uplift at 1, 3, and 10 years.

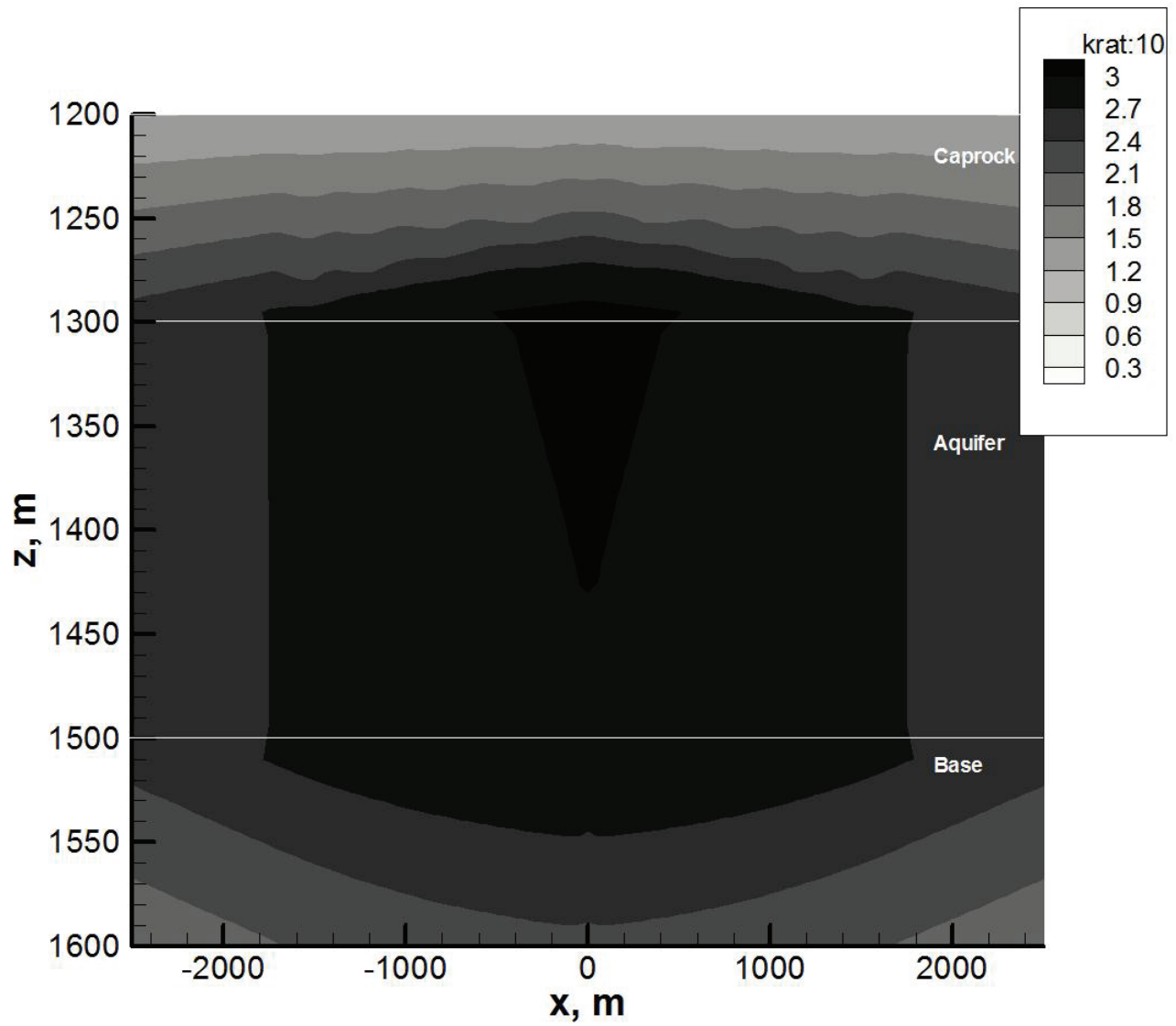


Figure 14: Permeability changes in the vicinity of the injector; modified Rutqvist and Tsang (2002) simulation using Porosity Option 1 from Table 1 and Permeability Option 1 from Table 2.

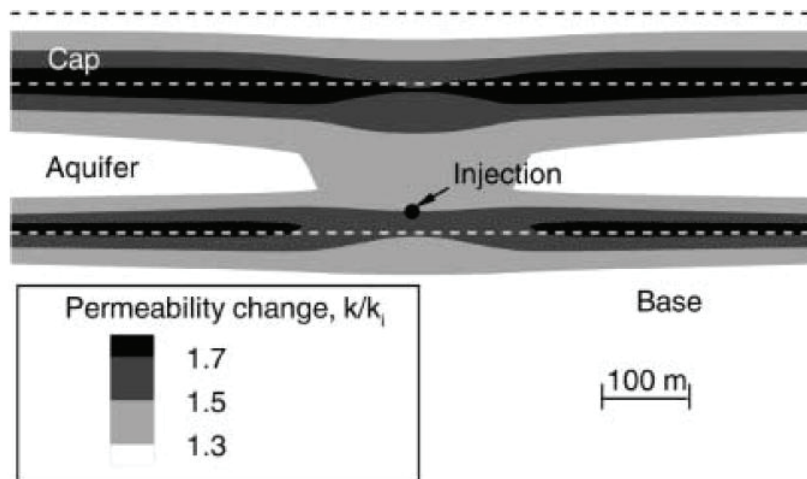


Figure 15: Rutqvist and Tsang (2002) permeability changes in the vicinity of the injector.

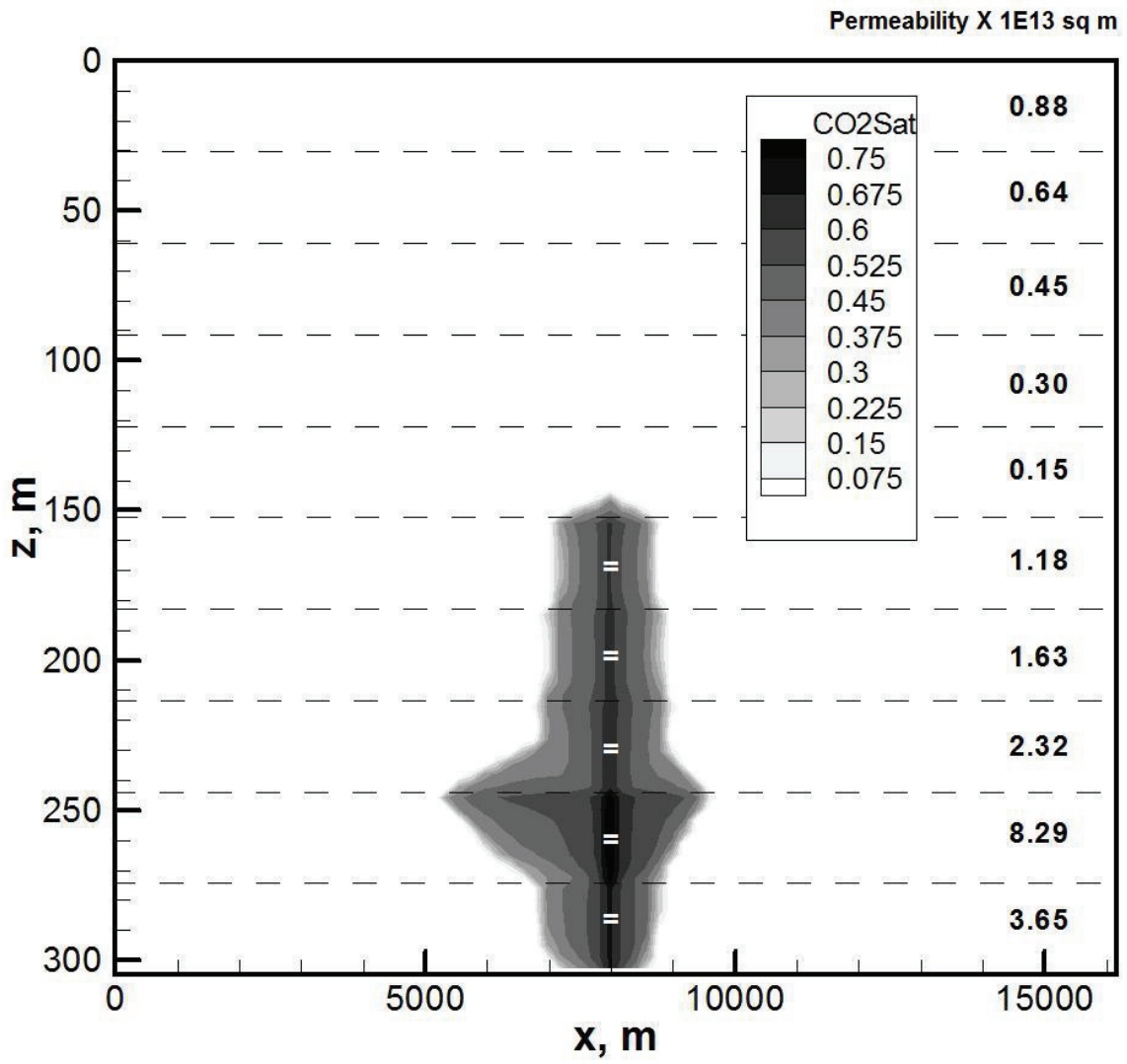


Figure 16: CO<sub>2</sub> saturation profile after 50 years of injection for cross section containing injection well; modified Kumar et al. (2005) simulation with finer grid.

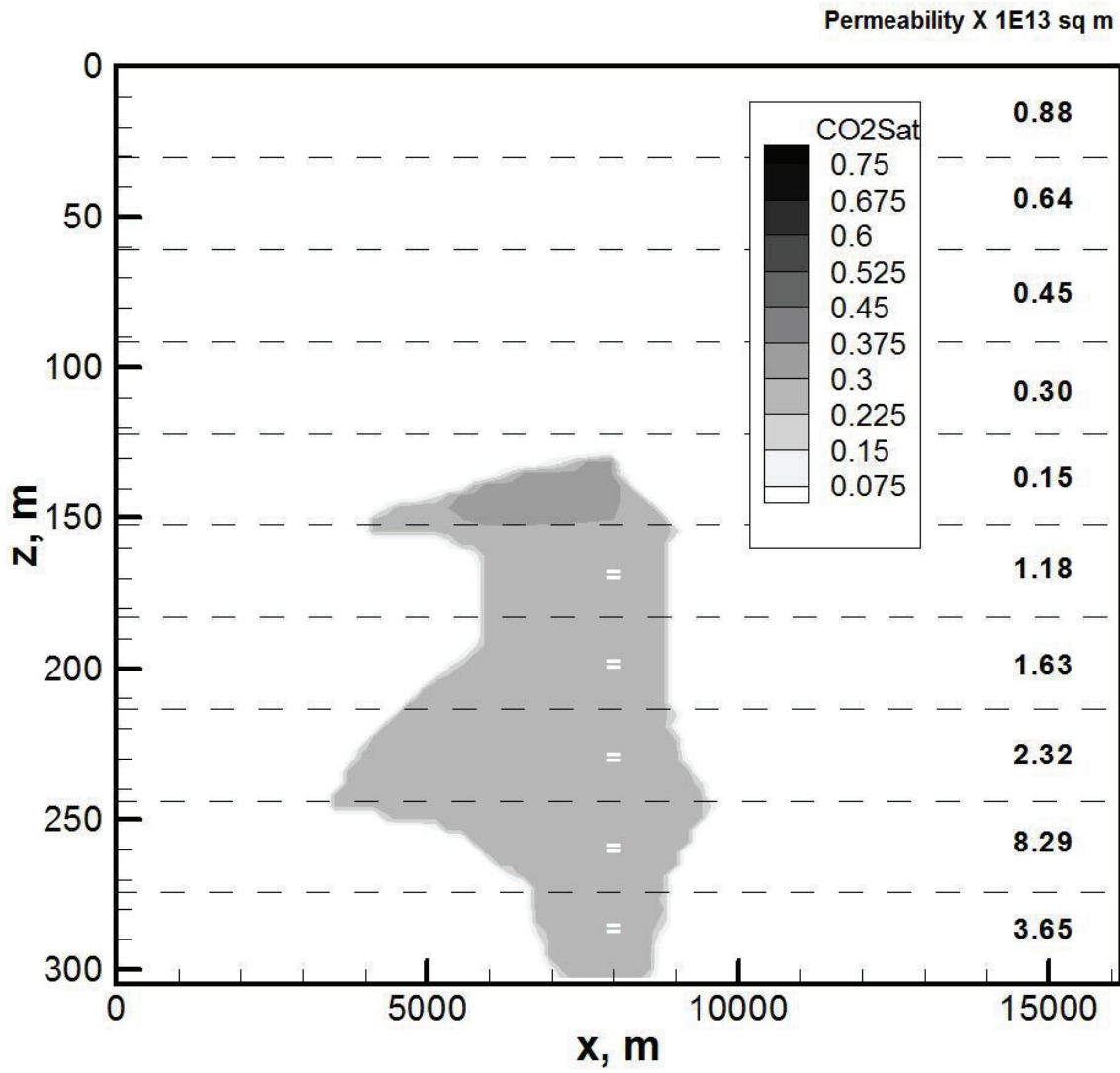


Figure 17: CO<sub>2</sub> saturation profile after 1,000 years of injection for cross section containing injection well; modified Kumar et al. (2005) simulation with finer grid.